

• State the main differences between geometric modeling and physical modeling

- h
- a. physical modeling is to general, a mathematical model describe the behavior of the system using simple physics laws with comparison to a simpler system. and we can test how the model will behave if we change some parameters.
- b. geom geometric modeling is a 3-D design shows the details of the object and you can animate it but you can't ~~and~~ calculate the forces or translation of it just a picture without physics ~~behind~~ behind it.

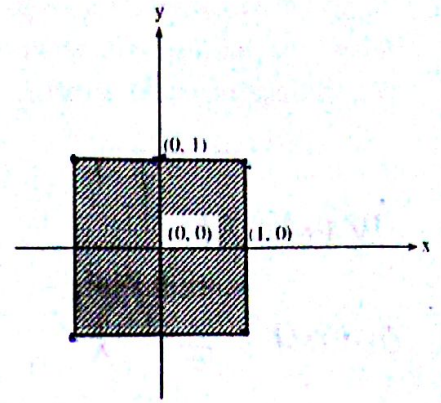
• List why a designer needs a CAD or CAM or CIM

- who? designer
- a. to help him in holding his imagination ~~and~~ ideas and knowledge in the design on the computer.
- b. manage & plan and control the production process with a direct or indirect interference.
- c. Improve the process by increases the quality, increases ^{Communication.} ~~communication~~ and increases the production.

• Define what is Modeling

- ~~It's using a physics laws to create mathematical describing for the system. with~~
- Using mathematical and physical equations and laws to compare the system with a simpler one. and to make changes to see what the results will be.
- ⌘

- Given the original shape and position of a square in following Figure.
- Find the configuration matrix C that represents the geometry
- Use uniform scaling (with respect to the origin) to magnify the object to three times its original size
- Find the position of vertices of the square when rotated +45 degrees (CCW)



①

$$C = \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

Last row

②

$$S_{cal} = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$C^* = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$C^* = \begin{bmatrix} 3 & 3 & -3 & -3 \\ 3 & -3 & -3 & 3 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

③

$$C^* = \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} \cos(45) & -\sin(45) \\ \sin(45) & \cos(45) \end{bmatrix}$$

$$C^* = \begin{bmatrix} \cos(45) & -\sin(45) \\ \sin(45) & \cos(45) \end{bmatrix} \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix}$$

For C^* after scaling.

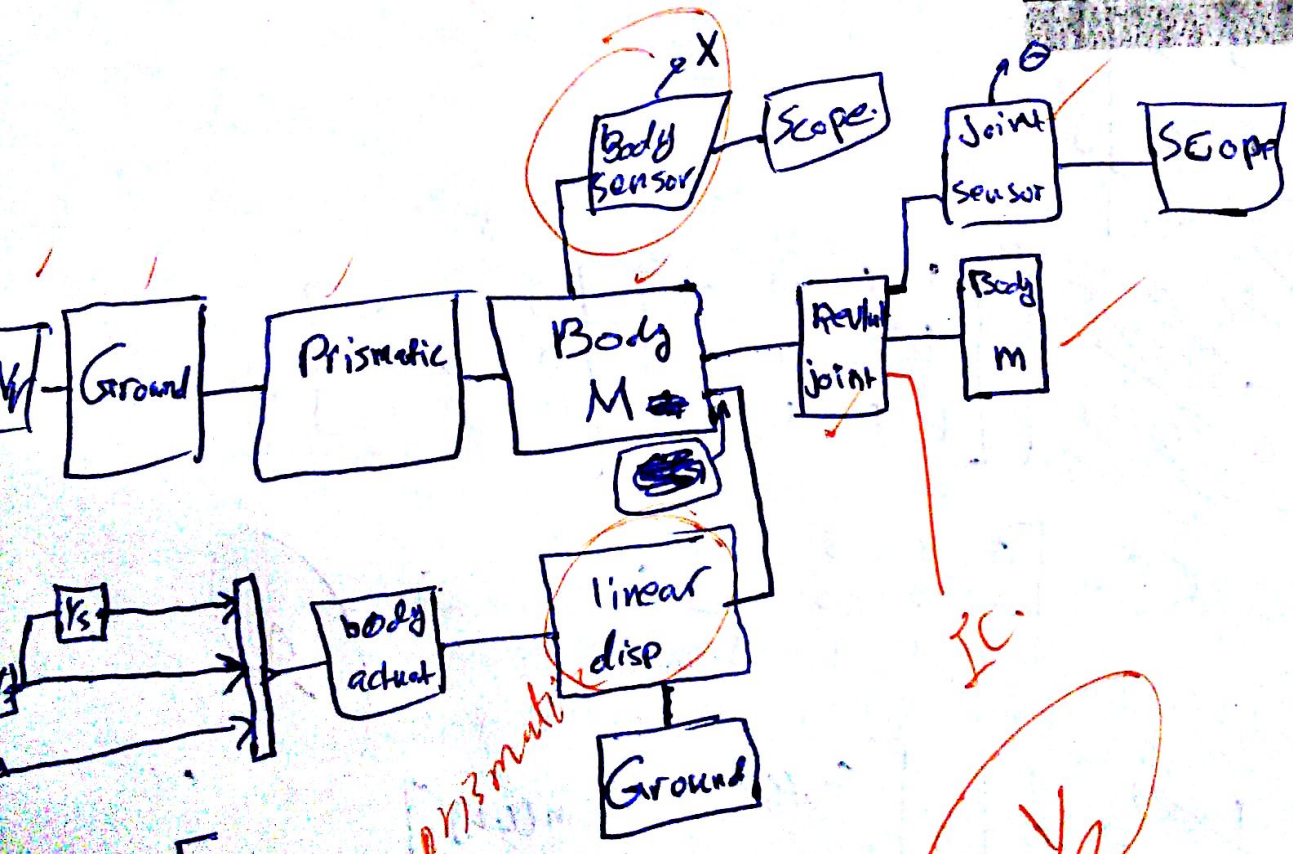
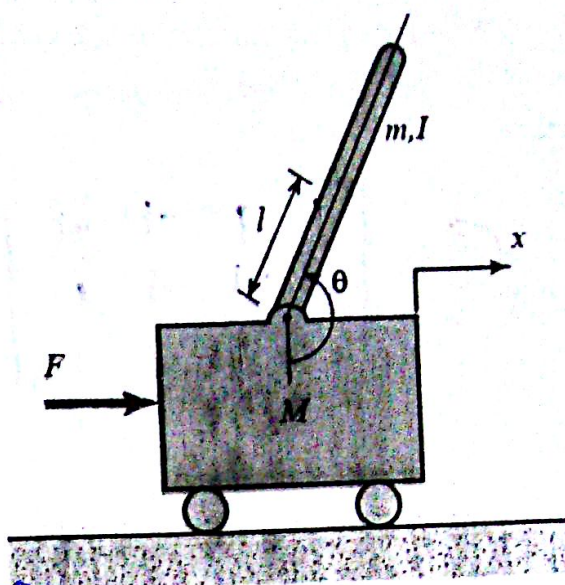
$$C^* = \begin{bmatrix} 0 & 1 & 0 & -1 \\ 1 & 0 & -1 & 0 \end{bmatrix} \cdot C^* = \begin{bmatrix} 0 & 3 & 0 & -3 \\ 3 & 0 & -3 & 0 \end{bmatrix}$$

where is rotation

Problem-3 (6pts)

- Consider a two-dimensional version of the inverted pendulum system with cart where the pendulum is constrained to move in the vertical plane shown in the figure below. For this system, the control input is the force F that moves the cart horizontally and the outputs are the angular position of the pendulum θ and the horizontal position of the cart x .

input F
output θ x



$$\Rightarrow a = \frac{F}{M + m}$$

$\frac{1}{2}$

friction