

Question 4

(4 Marks)

For the circuit shown in Figure 6, use mesh current analysis to find

- a- The mesh currents I_1 , I_2 , and I_3
- b- The current through the $30\ \Omega$ resistor.
- c- The power dissipated by the $15\ \Omega$ resistor.

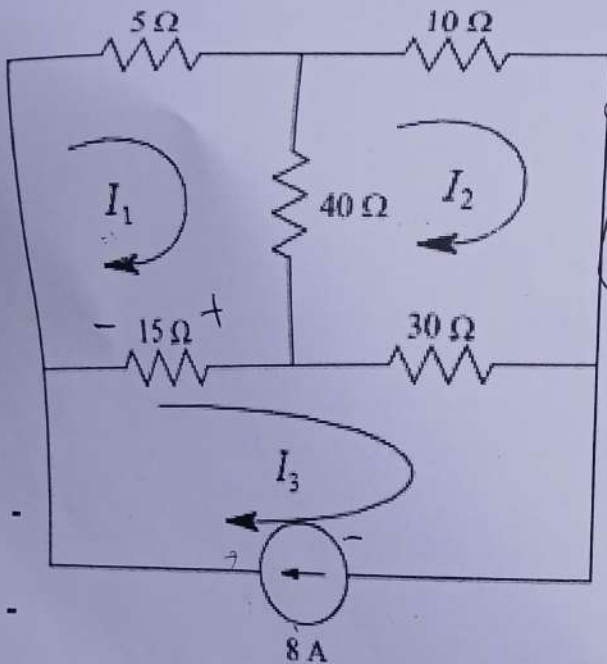


Figure 6:

at mesh ①

$$60I_1 + 15I_1 + 5I_1 - 40I_2 - 15I_3 = 0$$

$$60I_1 - 40I_2 - 15I_3 = 0$$

at mesh ②

$$10I_2 + 30I_2 + 40I_2 - 40I_1 - 30I_3 = 0$$

$$80I_2 - 40I_1 - 30I_3 = 0$$

at mesh ③

$$I_3 = 8$$

$$① \quad 60I_1 - 40I_2 = 120$$

$$② \quad 80I_2 - 40I_1 = 240$$

$$③ \quad I_3 = 8$$

$$I_1 = 6A$$

$$I_2 = 6A$$

$$I_3 = 8A$$

$$I_{30\Omega} = I_3 - I_2$$

$$8 - 6 = 2A$$

$$③ \quad I_{30\Omega} = 2A$$

$$P_{15\Omega} = I^2 R$$

$$= I(I R)$$

$$= (6)(6 \cdot 15)$$

$$④ \quad P_{15\Omega} = 540W$$

$$P_{15\Omega} = 540W$$

b- In Figure. 4, Find I_o/I_s

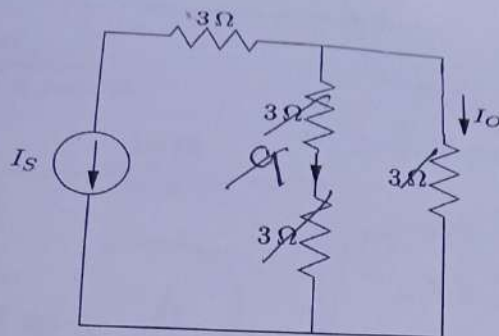
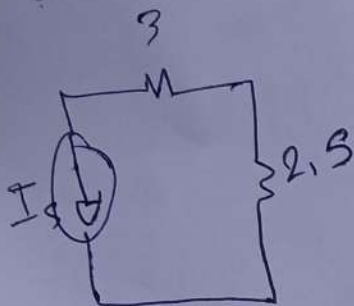


Figure 4:

$$I_s \Rightarrow \frac{I_o \times \frac{1}{3}}{\frac{2 \times \frac{1}{3}}{2 \times 3} + \frac{1}{6} + \frac{2 \times \frac{1}{3}}{2 \times 3}}$$



$$I_s = I_o$$

$$I_s = I_o \times \frac{1}{R} = I_s = I_o \times \frac{1}{\frac{5}{6}}$$

$$\frac{I_s}{6} = \frac{I_o}{I_s}$$

c- In the circuit shown in Figure. 5. Find V_o

$$\frac{I_{s15}}{I_s} = 6 \frac{I_o}{I_s}$$

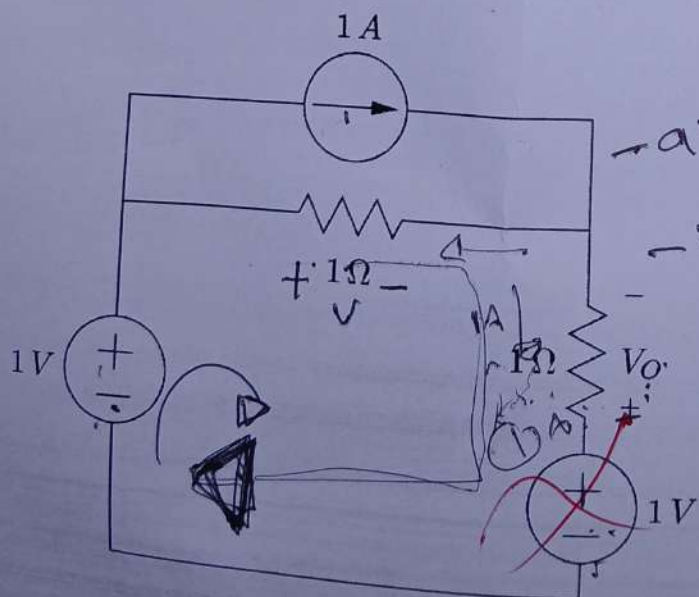
$$I_s = \frac{6 I_o \times \frac{1}{3} \times 3}{15}$$

$$I_s = \frac{6 I_o}{15}$$

$$V_o = \frac{V_o \times 1}{2}$$

$$V_o = \frac{V_o \times 1}{2}$$

$$V_o = 0$$



apply KVL

$$-1 - V_o + 1$$

$$V_o = 0$$

$$0.5$$

Figure 5:

$$I = \frac{V}{R} = \frac{1}{1} = 1$$

Question: 3

(6 Marks)

This question consist of 3 parts (2 marks each)

a- The equivalent resistance at the terminals a-b for the circuits shown in Figure. 3 is equal to

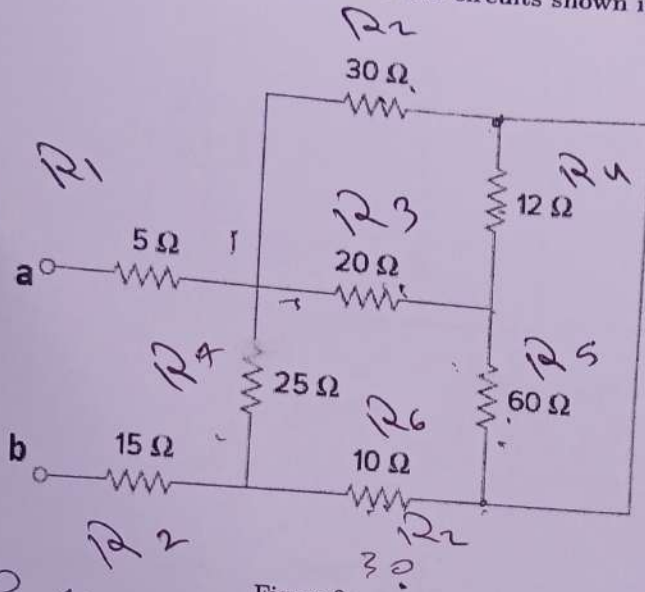
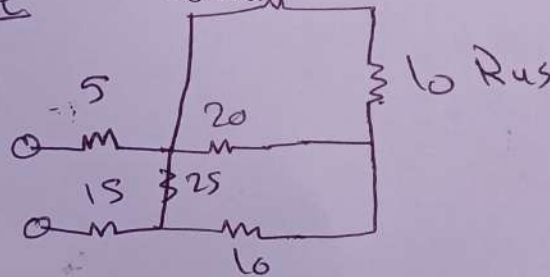


Figure 3:

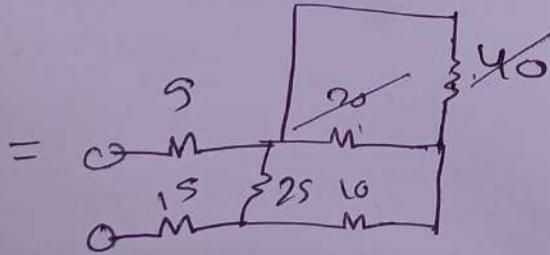


* R_4, R_5 ~~series~~ parallel

$$R_{45} = \frac{12 \times 60}{72} =$$

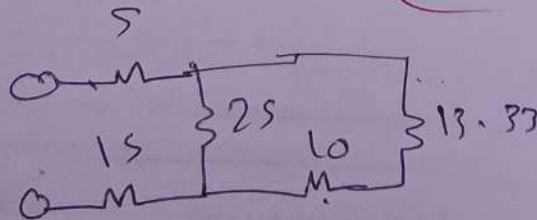
* R_{45}, R_2 series

$$80 + 10 = 40$$

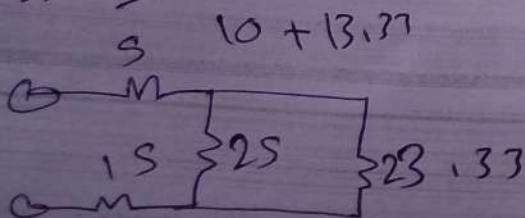


* R_{452}, R_3 ~~series~~ parallel

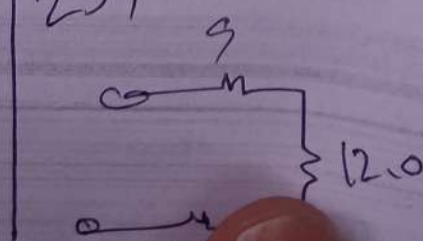
$$\frac{40 \times 20}{60} = 13.33$$



10, 13.33 parallel



25, 23.33 parallel



5, 12.0, 15 parallel

$$R_{eq} = 32$$

Question 2:

For the circuit shown in figure 2, Use the Nodal analysis method to find
a-The nodal voltages, V_1 and V_2 .
b-The current I_3
c-The power absorbed/ supplied by the current source.

(6 marks)

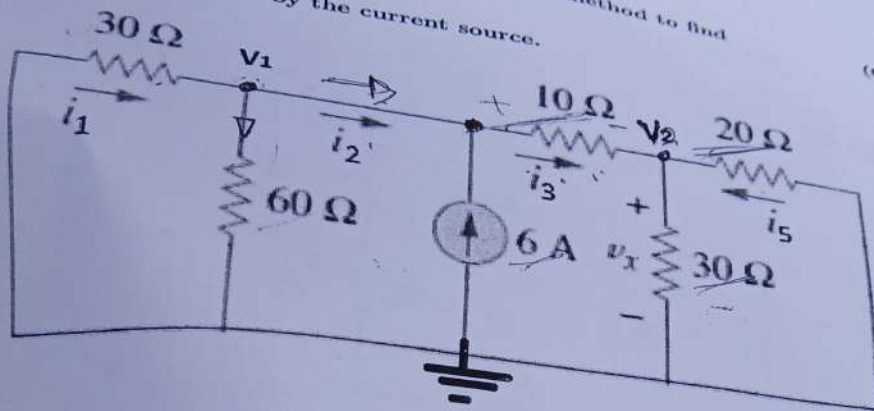


Figure 2:

at Node V_1 :- $\sum I_{in} = \sum I_{out}$

$$\frac{V_1}{30} = \frac{V_1}{60} + \frac{V_1 - V_2}{10} = \frac{V_1}{60} + \frac{V_1 - V_2}{6 \times 10} \quad \frac{2 \times V_1}{2 \times 30} = \frac{V_1}{30} + \frac{6V_1 - 6V_2 - 2V_1}{60}$$

at Node V_2 = $\frac{V_1 - V_2}{10} + \frac{V_2}{20} = \frac{V_2}{30}$ ~~$\frac{V_2}{30}$~~ = $\frac{5V_1 - 6V_2}{60}$

$$= \frac{6 \times V_1 - 6V_2}{6 \times 10} + \frac{3 \times V_2}{3 \times 20} - \frac{2 \times V_2}{2 \times 30} = 0$$

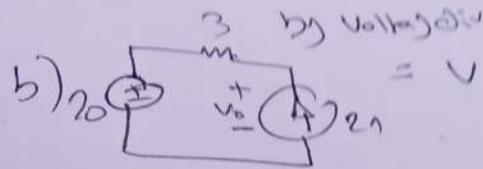
$$\frac{6V_1 - 6V_2 + 3V_2 - 2V_2}{60} = \frac{6V_1 - 5V_2}{60}$$

Question: 1

(4 Marks)

For the circuit shown in Figure 1 Find,
a- The mesh currents, I_1 and I_2
b- The voltage v across the current source

$$2 = 2I_1 + I_2$$



$$V = 4 \times 3 = 12$$

$$= 20 = V_0$$

$$V_0 = 20$$

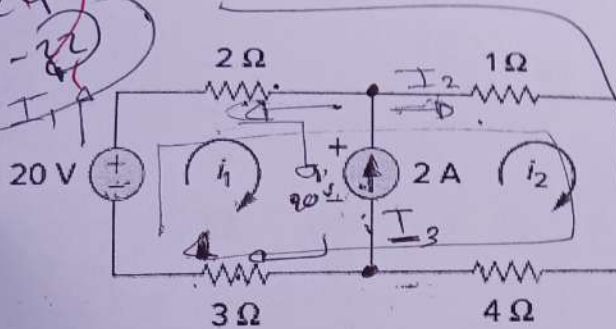
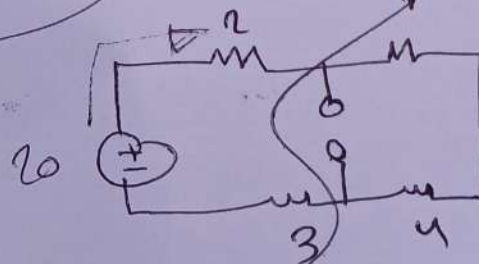
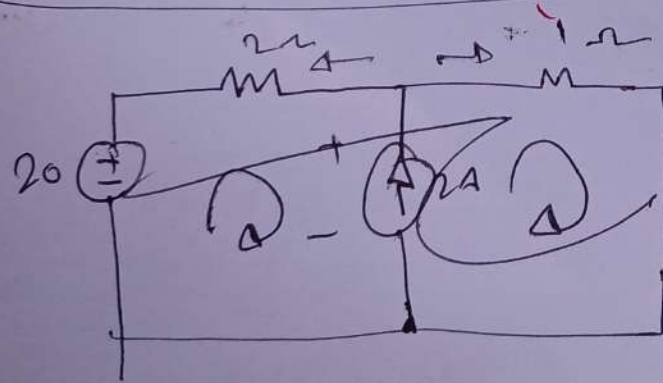


Figure 1:

Mesh (1) - $-20 + 2I_1 + 3I_1 - 2 = 2I_1 + 3I_1 - 2 = 0$

Mesh (2) - $2 + 1I_2 + 4I_2 - 2 = 5I_2 = 0$

Super Mesh - $-20 + 2I_1 + 1I_2 + 4I_2 - 2 = 0$



- apply KVL =

$$V = IR$$

$$= I \times R$$

$$2 = I(2 + 1 + 3 + 4)$$

$$2 = I \frac{10}{10}$$

$$I = 0.4$$

at mesh (1)
 $-20 + 2I_1 - 2 + 3I_1 - 2 = 0$

at mesh (2)
 $+2 + 1I_2 + 4I_2 - 2 = 0$